A Multiplexing Ripple Cancellation LED Driver With True Single-Stage Power Conversion and Flicker-Free Operation

Peng Fang ^(D), *Member, IEEE*, Samuel Webb ^(D), *Student Member, IEEE*, Yang Chen ^(D), *Member, IEEE*, Yan-Fei Liu ^(D), *Fellow, IEEE*, and Paresh C. Sen, *Life Fellow, IEEE*

Abstract—Although a single-stage off-line power light-emitting diode (LED) driver can achieve low cost and high efficiency, the notorious double-line-frequency flicker issue with a single-stage LED driver limits its usage in high-quality lighting applications. To solve lighting flicker, as well as maintain a low cost and high efficiency, a multiplexing ripple cancellation (MRC) LED driver is proposed in this paper. One switching cycle is divided into two intervals. During the first interval, the proposed LED driver operates as a conventional LED driver that transfers energy from the ac input to LED output, performs power factor correction, and generates the main output voltage. The main output voltage has a double-linefrequency ripple like in a conventional design. During the second interval, the proposed LED driver transfers energy from the ac input again to generate an opposite ripple voltage to cancel the ripple voltage from the main output. In this way, the voltage across the LED load is a dc to achieve flicker-free LED driving performance. More than 99% of the output power goes through one-time power conversion, while less than 1% goes through two-time power conversion. A 7.5-W experimental prototype is built and tested to verify the design concept.

Index Terms—Flicker-free operation, high power factor, multiplexing operation, off-line light-emitting diode (LED) driver, ripple cancellation.

I. INTRODUCTION

T HE light-emitting diode (LED) offers much higher efficacy than any other lighting devices and is one of the most promising new lighting technologies. High-quality LED light devices are more durable and provide comparable, if not better, light quality as other types of lighting. It has the potential to completely overtake other traditional light technologies, especially in residential applications. The global LED lighting

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P. Fang was with the Department of Electrical and Computer Engineering, Queen's University, Kingston, ON K7L 3N6, Canada. He is now with the Department of Electrical Engineering, University of Minnesota, Duluth, MN 55455 USA (e-mail: fangp@d.umn.edu).

S. Webb, Y. Chen, Y.-F. Liu, and P. C. Sen are with the Department of Electrical and Computer Engineering, Queen's University, Kingston, ON K7L 3N6, Canada (e-mail: 11sdw4@queensu.ca; yang.chen@queensu.ca; yanfei. liu@queensu.ca; senp@queensu.ca).

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market reached US\$ 26 billion in 2016 and is expected to reach US\$ 54 billion by 2022, growing at a rate of around 13% between 2017 and 2022 [1].

The LED driver, a specially designed power supply to regulate LED current, is the key technology in LED lighting, which determines the overall efficiency, lighting quality as well as the reliability of an LED lighting device. EnergyStar requires any ac connected LED driver to achieve a power factor higher than 0.9 for commercial applications or 0.7 for residential applications when its rated output power is greater than 5 W [2]. IEC-61000-3-2 further imposes limitations on input current harmonics for lighting device with more than 75 W rated output power. Complying with these requirements imposes great challenges on designing an ac-connected LED driver. The ac input power of an LED driver is a sinusoid-like waveform with a double-line-frequency ripple. A significant portion of the double-line-frequency ripple energy is usually passed to the LED load when a single-stage LED driver is used, which produces lighting flicker. It is well documented that lighting flicker at double-line-frequency is very harmful to our health, resulting in both short- and longterm health concerns [2]. The situation is much better when a two-stage LED driver is used. A two-stage LED driver can minimize the LED load ripple energy to a negligible level, achieving the so-called flicker-free operation. However, a two-stage LED driver has a much higher component cost and lower efficiency, which is extremely undesirable in cost-sensitive, low-power applications, for example, in LED light bulbs applications.

A great deal of research has been conducted in an attempt to design an LED driver that maintains the high efficiency and low cost of a single-stage solution, which also achieves the flicker-free operation of a two-stage LED driver. The energy buffering technologies [4]–[7] have been proposed to balance energy difference between ac input and LED output with a bidirectional dc–dc converter. The two-stage integrated methods [8]–[11] have been proposed to share components between the first PFC stage and the second dc–dc stage, which can reduce the component cost. The harmonic input currents injection method [12]–[14] have been proposed to minimize the double-linefrequency imbalanced energy existing in a single-stage LED driver. Therefore, the ripple LED current is reduced to alleviate lighting flicker.

The ripple cancellation method is proposed in [15]–[20]. A ripple cancellation converter is used in the designs to

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Fig. 1. Concept of the proposed MRC LED driver.

generate an opposite ripple voltage, which cancels the ripple voltage from the main output. As a result, a DC voltage is produced and applied to the LED load to achieve flicker-free LED driving performance. The greatest merits of this method are low component cost and high efficiency. The ripple cancellation converter processes only a small fraction of the total output power, which requires a minimal additional cost to implement and yields overall high efficiency. The energy-channeling LED driver is proposed in [20]. The input power is split into two portions, with the first major portion being transferred to the LED load and the second portion generating an opposite ripple voltage to achieve ripple cancellation. The great advantage of this solution is more than 98% of the output power go through one power conversion step, leading to an improved efficiency. One drawback of the energy-channeling LED driver is restricted operation. When a high power factor is achieved, the input power is a dc-biased sinusoidal waveform with a minimum value of zero. The energy available to sustain V_{o2} is from the input power and it will not be enough when the input power becomes very small. Complex auxiliary circuitry is needed to maintain proper operation of the energy-channeling LED driver. A multiplexing ripple cancellation (MRC) LED driver is proposed in this paper. It is also a true single-stage LED driver with 99.5% output power being processed once. It operates drastically different from the energy-channeling LED driver to free itself from the aforementioned limitation. In the new LED driver, the task of performing power factor correction and sustaining output V_{a2} are done in two separate intervals of one switching cycle. Therefore, sustaining the ripple cancellation voltage is independent of the power factor correction operation, and the aforementioned limitation in the energy-channeling LED driver is eliminated.

The remaining sections of this paper are organized as follows. Section II discusses the concept and operating principle of the proposed LED driver. Section III discusses the component voltage and current stresses. Section IV discusses the control strategy of the LED driver. Section V discusses the design considerations and an example design procedure. Different LED driving technologies are compared in Section VI. The experimental results of the proposed LED driver are presented in Section VI. Finally, the paper is concluded in Section VII.

II. CONCEPT AND OPERATING PRINCIPLE

Fig. 1 shows the operation concept of the proposed MRC LED driver. It operates in time multiplexing manner, with one

switching cycle being divided into two intervals, namely, interval I and interval II. During the time interval I, the power stage of the conceptual LED driver operates as a power factor correction (PFC) converter. Energy is transferred from the ac input to the main output V_{o1} and power factor correction is performed. During interval II, it operates as a ripple cancellation converter. The energy used to maintain V_{o2} is also from the ac input. The energy transferred from the ac input to both output V_{o1} and V_{o2} is done using a single-stage power conversion, which helps maintain a high efficiency comparable to a conventional single-stage LED driver. Although the proposed LED driver is validated with a 7.5-W experimental prototype, the same concept can be expandable for higher output power designs.

On the other side, the proposed LED driver has its own limitation, which is explained as follows. The current drawn from the ac input (after input bridge rectifier) during the interval I operation is named as I_{in_T1} and the current drawn from the ac input during the interval II operation is named as I_{In_T2} . I_{in_T1} follows the input voltage to achieve the power factor correction and can be expressed as

$$I_{in_T1}(t) = V_{in_rec}(t) \times k \tag{1}$$

where k is a constant coefficient between the input voltage and $I_{in T1}$ in (1). During interval II, the power needed to maintain V_{o2} is also supplied from the ac input. Therefore, $I_{in T2}$ can be expressed as

$$I_{in_T2}(t) = \frac{V_{o2}(t) \times I_{\text{LED}}}{V_{in_rec}(t)}.$$
(2)

As indicated by (2), $I_{in,T2}$ does not follow the input voltage. Therefore, the overall ac input current is not an ideal sinusoidal waveform. To minimize the harmonic currents from $I_{in,T2}$, it should be kept as small as possible, which can be achieved by reducing the output voltage V_{o2} .

In addition, (2) also indicates that $I_{in_T2}(t)$ will approach infinity when $V_{in}(t)$ drops to zero. Therefore, to curb the ac input current during the ac input voltage zero-crossing, the input voltage should be limited to a minimal level instead of dropping to zero. A voltage source V_{aux} can be added after the bridge rectifier and the minimum input voltage after input rectifier becomes

$$V_{in_rec_\min} = V_{aux}.$$
 (3)

 V_{aux} can be separated from the input bus with a diode D_s that is shown in Fig. 1. When $|V_{in}(t)| > V_{\text{aux}}$, the diode D_s is reversely biased and the energy is taken from the ac input. When $|V_{in}(t)| < V_{\text{aux}}$, the bridge rectifier diodes are reversely biased, during which D_s conducts current and the energy is supplied by V_{aux} . The ac input current becomes zero during this period. It should note that, as an autonomous system, V_{aux} is also generated by the power circuit of the LED driver. V_{aux} can be generated in flyback mode energy transfer fashion. By addition of another winding in the inductor and orienting it in the same way as that of the main winding N_1 , a voltage can be developed on the new winding when the diode D_1 is conducting, and this voltage is a scaled reflection of the output V_{o1} , with the value determined by the turns ratio between N_1 and the new winding.



Fig. 2. Critical line cycle waveforms of the proposed MRC LED driver.

A dc voltage can be generated by rectifying the winding voltage with a diode.

Also, it can be understood that the energy supplied by V_{aux} goes through two power conversion steps. First, the energy is transferred from the ac input to V_{aux} . Second, the energy is transferred from V_{aux} to the LED load. As mentioned, one key feature of the proposed MRC LED driver is to achieve single-stage power conversion. The following measure is adopted to minimize the amount of energy going through two times power conversion—once V_{aux} kicks in to supply the energy, the interval I operation is temporary disabled. Therefore, V_{aux} only supplies energy to V_{o2} through the interval II operation, which is typically less than 1% of the total energy delivered to the LED load, as will be analyzed later.

The key line cycle waveforms of the proposed MRC LED driver are shown in Fig. 2. When $|V_{in}| > V_{aux}$, the time interval I, the ac input current I_{in_T1} follows the input voltage. When $|V_{in}| < V_{aux}$, I_{in_T1} is zero as the time interval I operation is disabled under this condition. The current I_{in_T2} is provided by the voltage source V_{aux} . The time interval I input power P_{in_T1} is a dc-biased sinusoidal waveform with a zero-power region when $|V_{in}| < V_{aux}$. Similar to a conventional PFC, the ripple power of P_{ph1} produces a ripple voltage on the main output V_{o1} and the ripple voltage of V_{o1} is approximately 90° lagging the double-line-frequency ripple of P_{in_T1} . To achieve cancellation, the double-line-frequency ripple voltage of V_{o2} is made to be opposite to that of V_{o1} . The amount of energy transferred by V_{aux} can be expressed as

$$E_{\rm aux} = \int_{t_a}^{t_b} V_{o2}(t) \times I_{\rm LED} \tag{4}$$

where E_{aux} represents the energy provided by V_{aux} in a half line cycle and t_a and t_b represent the beginning and the end points when $|V_{in}| < V_{\text{aux}}$. Since the output V_{o2} stays around the average value when $|V_{in}| < V_{\text{aux}}$, (4) can be further simplified as

$$E_{\text{aux}} \approx V_{o2_avg} \times I_{\text{LED}} \times (t_b - t_a).$$
(5)

The time $(t_b - t_a)$ can be calculated as

$$t_b - t_a = \frac{\arcsin\left(\frac{V_{\text{aux}}}{V_{in,pk}}\right)}{\pi} \times T_{\text{line}}.$$
 (6)



Fig. 3. Circuit implementation of the MRC LED driver based on the buck-boost topology.

Combining (5) and (6) yields

$$E_{\text{aux}} \approx V_{o2_avg} \times I_{\text{LED}} \times \frac{\arcsin\left(\frac{V_{\text{aux}}}{V_{in_pk}}\right)}{\pi} \times T_{\text{line}}.$$
 (7)

 (t_b-t_a) is calculated to be 1.03 ms when $V_{aux} = 30$ V and $V_{in} = 110$ Vrms. Using $V_{o2_avg} = 2.5$ V and $I_{LED} = 0.15$ A, E_{aux} is calculated to be 2.5 V × 0.15 A × 1.03 ms = 0.39 mJ. The total energy delivered to the LED load in a half line cycle is 7.5 W × $(2f_{line}) = 62.5$ mJ. Therefore, only 0.6% of the total energy is processed twice and 99.4% of the energy goes through the single-stage power conversion. Thus, the proposed LED driver can be reasonably said to operate as a single-stage LED driver.

The limitation of the proposed MRC LED driver, as discussed earlier, is the harmonic currents introduced by the time interval II operation and by the ac input current zero-crossing distortion. More discussion will be presented in Section V to investigate the limitation of the proposed MRC LED driver and a design guideline to reduce harmonics current will be provided to comply with IEC-61000-3-2 for designs with greater than 75 W output power.

Fig. 3 shows a buck-boost topology-based implementation of the MRC LED driver. The same concept can be implemented with other current-fed topologies, such as flyback and boost. Compared to a conventional buck-boost LED driver, the proposed MRC LED driver contains an additional ripple cancellation unit (RCU) and the input voltage clamp unit, which are both highlighted in Fig. 3. The RCU is active during the interval II operation, through which an opposite ripple voltage is produced. It will be discussed in Section IV that the voltage stresses of D_2 and Q_2 are very low (around 20 V) so that low voltage rating devices can be used to maintain an overall low cost. As the energy processed by V_{aux} is around 0.5% of the overall output power, very low-cost components can be used to generate V_{aux} , which will not contribute too much cost. The same is also true with D_s , which provides current flow path when V_{aux} provides energy. On the contrary, the second-stage dc-dc converter needs to process 100% of output power. Therefore, the cost to implement the second-stage dc-dc converter in a two-stage design is much greater. In addition, the proposed LED driver does not need an extra inductor to generate the ripple cancellation voltage, which also helps to save cost.

To facilitate a better understanding of the structure of the proposed MRC LED driver, its equivalent circuits during the



Fig. 4. Equivalent circuits of the MRC LED driver. (a) Interval I circuit. (b) Interval II circuit.

interval I and the interval II operations are shown in Fig. 4. During the interval I operation, the equivalent circuit is operated as an independent buck–boost PFC converter. During the interval II operation, the equivalent circuit is operated as an independent flyback converter. Fig. 5 shows one switching cycle operation of the MRC LED driver. The time interval I operation is further divided into two time intervals $[t_0-t_1]$ and $[t_1-t_2]$, and the time interval II operation is further divided into intervals $[t_2-t_3]$ and $[t_3-t_4]$. Note that the voltage V_{aux} and D_3 are not shown in Figs. 4 and 5 for succinctness.

The critical switching waveforms in one switching cycle is shown in Fig. 6. The following brief analysis explains how power factor correction is performed during the time interval I operation. The switching current starts from zero at the beginning of the time interval I operation. The ON time of the interval I operation $[t_0-t_1]$ is a constant in a half line cycle. The interval II operation will not start until the switching current I_{D1} drops to zero. At the end of time interval II operation, switching current I_{D2} also drops to zero. The switching period is constant in every switching cycle. The detailed switching operation in each time interval will be discussed as follows.

A. Time $[t_0-t_1]$

A switching cycle starts at time t_0 when MOSFET Q_1 is turned ON. The inductor is charged by the rectified ac input. The switching current, in winding N_1 , starts rising from zero and increases linearly with the turn on time. The switching current in winding N_1 (and Q_1) peaks at time t_1 right before Q_1 is turned OFF and can be expressed as

$$I_{Q_1,t_1} = \frac{V_{\text{in}} \times (t_1 - t_0)}{L_{N1}}.$$
(8)

The average current drawn from the ac input during time interval I operation can be expressed as

$$I_{in_T1_avg} = \frac{I_{Q1_t_1} \times (t_1 - t_0)}{2T_s}$$
(9)

where $I_{in_T1_avg}$ represents the average input current in a switching cycle during the interval I operation. Further combining (8) and (9) yields

$$I_{in_T1_avg} = \frac{V_{in} \times (t_1 - t_0)^2}{2 \times T_s \times L_{N1}}.$$
 (10)

As both the terms (t_1-t_0) and T_s are constant in a half line cycle, $I_{in_T 1_avg}$ is therefore proportional to the input voltage. Because of the opposite winding orientation between N_1 and N_2 , both diodes D_1 and D_2 are reversely biased and there is no current in winding N_2 . The body diode of MOSFET Q_2 is forward biased. The voltage stresses on D_1 and D_2 during this time interval can be expressed as

$$V_{D_1[t_0-t_1]} = V_{o1} + V_{\rm in} \tag{11}$$

$$V_{D_2[t_0 - t_1]} = V_{o2} + V_{in} \times \frac{N_2}{N_1}.$$
 (12)

B. Time $[t_1-t_2]$

As MOSFET Q_1 is turned OFF at time t_1 , the magnetic current in winding N_1 is forced to conduct in diode D_1 . The voltage across winding N_1 is clamped to be the same as the output V_{o1} (ignoring the forward voltage drop of diode D_1). The voltage across MOSFET Q_1 is the sum of the input voltage and the output voltage V_{o1} and is expressed as

$$V_{Q_1[t_1-t_2]} = V_{\rm in} + V_{o1}.$$
 (13)

During this time interval, the energy stored in the inductor is transferred to the output V_{o1} . The magnetic current in winding N_1 starts decreasing at time t_1 and becomes zero at time t_2 , which ends the interval I operation. One should note that during this time interval, the voltage on winding $N_2 V_{N2[t1-t2]}$ is designed to be higher than V_{o2} as shown

$$V_{N_2[t_1-t_2]} = V_{o1} \times \frac{N_2}{N_1} > V_{o2}.$$
 (14)

Therefore, the diode D_2 is forward biased while the body diode of Q_2 is reversely biased. The voltage across the drain to source terminals of Q_2 can be expressed as

$$V_{Q_2[t_1-t_2]} = V_{N_2[t_1-t_2]} - V_{o2} = V_{o1} \times \frac{N_2}{N_1} - V_{o2}.$$
 (15)

C. Time $[t_2-t_3]$

The time interval II operation starts at time t_2 and MOSFET Q_1 is turned ON again. The voltage stresses on these power components are the same as they are during the time interval $[t_0-t_1]$. The inductor current in MOSFET Q_1 peaks at t_3 again before Q_1 is turned OFF. The switching current in Q_1 at t_3 is expressed as

$$I_{Q_1,t_3} = \frac{V_{\rm in} \times (t_3 - t_2)}{L_{N1}}.$$
 (16)

MOSFET Q_2 is designed to be turned ON at t_2 . Theoretically, MOSFET Q_2 can be turned ON anywhere within $[t_2-t_3]$ without affecting the expected operation.



Fig. 5. One switching cycle operation of the proposed MRC LED driver. (a) $[t_0 - t_1]$. (b) $[t_1 - t_2]$. (c) $[t_2 - t_3]$. (d) $[t_3 - t_4]$. (e) $[t_4 - t_5]$.



Fig. 6. Key switching current waveforms of the proposed MRC LED driver.

D. Time $[t_3-t_4]$

When MOSFET Q_1 is turned OFF at t_3 , the magnetic inductor current needs to find another path to continue the current flow. As Q_2 is already on, both winding N_1 and N_2 provide current flowing paths. The turns ratio $N_1:N_2$ in the proposed design forces the magnetic current to continue flowing in the winding N_2 and the explanation is as follows. If the magnetic current conducts in winding N_2 , the voltage across the winding N_2 is clamped at V_{o2} (with ignoring the forward voltage drop of D_2). The voltage reflected on the winding N_1 becomes

$$V_{N_1[t_3 - t_4]} = V_{o2} \times \frac{N_2}{N_1}.$$
(17)

Combining (14) and (17) yields

$$V_{N_1[t_3 - t_4]} < V_{o1}. \tag{18}$$

Equation (18) indicates that the voltage potential at the anode of D_1 is smaller than the voltage potential at the cathode of D_1 . Therefore, the diode D_1 is reversely biased. Therefore, the aforementioned assumption is valid and the magnetic current only conducts in winding N_2 during $[t_3-t_4]$. The inductor releases the stored energy to the output V_{o2} during the time interval $[t_3-t_4]$. The magnetic current in winding N_2 starts decreasing from t_3 and it drops to zero at time t_4 , which ends the time interval II operation. There is a voltage falling on MOSFET Q_1 again, which can be expressed as

$$V_{Q_1[t_3-t_4]} = V_{\rm in} + V_{o2} \times \frac{N_1}{N_2}.$$
 (19)

E. Time $[t_4-t_5]$

There is a small time interval $[t_4-t_5]$ to maintain the DCM operation. There is no active energy transfer during this time interval and the magnetic current in the inductor remains zero.

	Q1	D_1	Q2	D2	
[t ₀ -t ₁]	0	$V_{in} + V_{o1}$	0	$V_{o2} + V_{in} \times \frac{N_2}{N_1}$	
[t ₁ -t ₂]	$V_{in} + V_{o1}$	0	$V_{o1} imes rac{{N_2}}{{N_1}} - V_{o2}$	0	
[t ₂ -t ₃]	0	$V_{in} + V_{o1}$	0	$V_{o2} + V_{in} \times \frac{N_2}{N_1}$	
[t3-t4]	$V_{in} + V_{o2} \times \frac{N_1}{N_2}$	$V_{o1} - V_{o2} \times \frac{N_1}{N_2}$	0	0	
Max	$V_{in} + V_{o1}$	$V_{in} + V_{o1}$	$V_{o1} \!\times\! \frac{N_2}{N_1} \!-\! V_{o2}$	$V_{o2} + V_{in} \times \frac{N_2}{N_1}$	

III. VOLTAGE AND CURRENT STRESSES ANALYSIS

As the switching operation has been discussed, the maximum voltage stress of each component in one switching cycle is summarized in Table I.

The maximum voltage across the drain and the source terminals of Q_1 and the reverse voltage across the diode D_1 in a half line cycle occur when the input voltage reaches the maximum in a half line cycle. Therefore, the maximum voltage stresses can be calculated as

$$V_{Q1_ds_max} = V_{D1_max} = |V_{in}|_{max} + V_{o1}$$
 (20)

The maximum reverse voltage across the drain and the source terminals of D_2 in a half line cycle can be expressed as

$$V_{Q2_ds_max} = V_{o1_max} \times \frac{N_2}{N_1} - V_{o2_min}.$$
 (21)

The maximum voltage across diode D_2 in a half line cycle can be expressed as

$$V_{D2_max} = |V_{in}|_{max} \times \frac{N_2}{N_1} + V_{o2_avg}$$
 (22)

Under the condition $V_{in} = 110$ Vrms, $N_1:N_2 = 8:1$, $V_{o1_max} = 49$ V, $V_{o1_min} = 47$ V, $V_{o2_max} = 3$ V, $V_{o2_min} = 1$ V, the maximum voltage across the drain to source terminals of Q_1 and the reverse voltage on D_1 are calculated to be 203 V, the reverse voltage across diode Q_2 is calculated to be 5.25 V, and the voltage across the drain to source terminals of Q_2 is calculated to be around 22 V.

The current stresses of these components in one switching cycle is summarized in Table II. The current stresses of these components cannot be calculated from the expression in Table II since the timespans (t_1-t_0) and (t_3-t_2) are unknown yet. Further derivation is needed to find the mathematical expressions for the component current stresses. The timespans (t_1-t_0) , $(t_2 \cdot t_1)$, (t_3-t_2) , and (t_4-t_3) will also be derived.

To calculate the current stresses of these components, the time intervals (t_1-t_0) and (t_3-t_2) need to be calculated as well. In a half line cycle, the root-mean-square (rms) value of the time interval I input current $I_{in_T I_1 rm_s}$ can be expressed as

$$I_{ph1_rms} = \frac{P_{ph1_avg}}{V_{in_rms}}$$
(23)

where (23) P_{ph1_avg} represents the average time interval I input power. The constant coefficient k between the input voltage and

TABLE II MRC LEDS DRIVER COMPONENTS CURRENT STRESSES

	Q1	D_1
At t ₁	$\frac{V_{in} \times (t_1 - t_0)}{L_{_{N1}}}$	$\frac{V_{in} \times (t_1 - t_0)}{L_{N1}}$
At t ₃	$\frac{V_{in} \times (t_2 - t_3)}{L_{N1}}$	0
Max	$Max\left\{\frac{V_{in} \times (t_1 - t_0)}{L_{N1}}, \frac{V_{in} \times (t_2 - t_3)}{L_{N1}}\right\}$	$\frac{V_{in} \times (t_1 - t_0)}{L_{N1}}$
	Q2	D_2
At t ₃	$\frac{V_{in} \times (t_2 - t_3)}{L_{N1}} \times \frac{N_1}{N_2}$	$\frac{V_{in} \times (t_2 - t_3)}{L_{N1}} \times \frac{N_1}{N_2}$
Max	$Max\left\{\frac{V_{in} \times (t_1 - t_0)}{L_{N1}}, \frac{V_{in} \times (t_2 - t_3)}{L_{N1}} \times \frac{N_1}{N_2}\right\}$	$\frac{V_{in} \times (t_2 - t_3)}{L_{N1}} \times \frac{N_1}{N_2}$

the time interval I input current can be expressed as

$$k = \frac{I_{ph1_avg}}{V_{\rm in}}.$$
(24)

Combining (10) and (24) yields

$$k = \frac{(t_1 - t_0)^2}{2 \times T_s \times L_{N1}}.$$
 (25)

The coefficient k can be also expressed as

$$k = \frac{I_{ph1_rms}}{V_{in_rms}}.$$
(26)

Combining (23), (25), and (26) yields

$$(t_1 - t_0) = \frac{1}{V_{in_rms}} \sqrt{2 \times P_{ph1_avg} \times T_s \times L_{N1}}.$$
 (27)

Combining (8) and (27), the switching current in Q_1 at time t_1 can be expresses as

$$I_{Q1_t1} = \frac{V_{in_rec}}{V_{in_rms}} \sqrt{\frac{2 \times P_{ph1_avg} \times T_s}{L_{N1}}}.$$
 (28)

With the voltage-second balance law, one can also get

$$(t_2 - t_1) = (t_1 - t_0) \times \frac{V_{\text{in}}}{V_{o1}}.$$
 (29)

Substituting (27) into (29) yields

$$(t_2 - t_1) = \frac{V_{in_rec}}{V_{o1}} \times \frac{1}{V_{in_rms}} \sqrt{2 \times P_{ph1_avg} \times T_s \times L_{N1}}.$$
(30)

The energy supplied from the ac input during the time interval II operation is equal to the energy delivered to the LED load via output V_{o2} in every switching cycle. Therefore, the following relationship is valid:

$$\frac{1}{2} \times I_{D_2 t_3}^2 \times L_{N2} = P_{o2} \times T_s = I_{\text{LED}} \times V_{o2} \times T_s.$$
(31)

Rearranging (31) yields

$$I_{D_2,t_3} = I_{Q_2,t_3} = \sqrt{\frac{2 \times I_{\text{LED}} \times V_{o2} \times T_s}{L_{N2}}}$$
$$= \sqrt{\frac{2 \times I_{\text{LED}} \times V_{o2} \times T_s}{L_{N1}}} \left(\frac{N_1}{N_2}\right).$$
(32)

The switching current reflects to the winding N_1 at time t_3 can, therefore, be written as

$$I_{N_1,t_3} = I_{Q_1,t_3} = \sqrt{\frac{2 \times I_{\text{LED}} \times V_{o2} \times T_s}{L_{N1}}}.$$
 (33)

Substituting (33) into (16) yields

$$(t_3 - t_2) = \frac{1}{V_{in_rec}} \times \sqrt{2 \times I_{\text{LED}} \times V_{o2} \times T_s \times L_{N1}}.$$
 (34)

One should note that $V_{in_rec} = 0$ should not be used to calculate (t_3-t_2) as the minimum value of V_{in_rec} is V_{aux} . According to the voltage–second balance law, the time (t_4-t_3) can be expressed as

$$(t_4 - t_3) = (t_3 - t_2) \times \frac{V_{in_rec}}{V_{o2}} \times \frac{N_2}{N_1}.$$
 (35)

Substituting (34) into (35) yields

$$(t_4 - t_3) = \sqrt{\frac{2 \times I_{\text{LED}} \times T_s \times L_{N1}}{V_{o2}}} \times \frac{N_2}{N_1}.$$
 (36)

Although the switching current in Q_1 peaks at t_1 and t_3 in one switching cycle, it is found that the maximum current in Q_1 occurs at t_1 when V_{in} is at the maximum in a half line cycle, which can be explained as follows. The square of $I_{Q1,t1}$ is proportional to the time interval I input power and the square of $I_{Q1,t3}$ is proportional to the time interval II input power. The maximum time interval I input power is far higher than the maximum of time interval II input power. Therefore, the maximum switching current in Q_1 occurs at t_1 of a switching cycle when the ac input voltage and the time interval I input power are also at their maximum.

By replacing V_{in_rec} with $V_{in_rec_max}$ in (28), the maximum peak switching current in Q_1 and D_1 is calculated to be 1.09 A under the condition $P_{ph1_avg} = 7.5$ W, $V_{in_rms} = 110$ Vrms, $N_1:N_2 = 8:1, L_{N1} = 1.25$ mH, By replacing V_{o2} with V_{o2_max} in (32), the maximum switching current in Q_2 and D_2 is calculated to be 1.51 A under the condition $V_{o2_max} = 3$ V, $I_{LED} = 0.15$ A, $N_1:N_2 = 8:1$, and $L_{N1} = 1.25$ mH.

IV. CONTROL SCHEME

Fig. 7 shows the control diagram of the proposed MRC LED driver. Two control loops are needed for the LED driver, namely, the LED current feedback loop and the output V_{o2} voltage loop.

To achieve LED current regulation, the LED current is sensed and compared with its current reference. The compensated error signal, V_{ctrl1} , is compared with the sawtooth signal to generate the gate driving signal for MOSFET Q_1 during the interval I operation. Under steady state, V_{ctrl1} is a constant in a half line cycle. Therefore, the ON time of Q_1 during phase one (t_1-t_0) is constant. Under discontinuous conduction mode and flyback topology, the interval I input current automatically follows the input voltage to perform the power factor correction [33]. When the sensed input current is not equal to the LED current reference, V_{ctrl1} will be changed automatically by the feedback loop. Therefore, (t_1-t_0) and the rms input current will change. The change in the rms input current lead to change in the input power and the output voltage V_{o1} . V_{o1} will settle to the value



Fig. 7. Control diagram of the proposed MRC LED driver.

that produces the exact LED current required by its reference. It should be noted that the average voltage V_{o2} is a constant, and it is not a part of the LED current regulation loop.

To achieve ripple cancellation, the output voltage V_{o1} is sensed by the low-frequency sensing (LFS) circuit to extract the double-line-frequency ripple voltage. The sensed ripple voltage becomes the reference voltage of $V_{o2,ref}$. The output voltage V_{o2} is sensed and compared with this reference. The compensated error voltage V_{ctrl2} is compared with the sawtooth signal to produce the gate driving signal of Q_1 during the interval II operation. The voltage loop used to regulate $V_{\alpha 2}$ should have a high enough bandwidth (>10 kHz) to achieve close tracking of the reference voltage. In the experimental prototype, a type II compensation with ~ 10 kHz bandwidth is used in the regulation loop for V_{o2} . There is also logic required to control the gate driving of Q_1 . When $|V_{in}| < V_{aux}$, the gate driving of Q_1 during the interval I operation is disabled. In this way, no energy is delivered to the output V_{o1} during this period, minimizing the amount of energy going through two power conversion steps.

Fig. 8 shows how to generate the gate driving pulse for Q_1 and Q_2 . The control signals V_{ctrl1} and V_{ctrl2} are compared with the same sawtooth signal to generate the gate driving G_{Q1} and G_{Q2} for Q_1 and Q_2 . At time t_0 , the beginning of a switching cycle, Q_1 is turned ON and the inductor current in winding N_1 starts increasing. At time t_1 , the control signal V_{ctrl1} and the sawtooth signal crossover, which terminates the ON period of G_{Q1} . The inductor current starts decreasing and transferring energy to the output V_{o1} . At time t_2 , the inductor current drops to zero, which triggers the turn-ON of Q_1 again. Q_2 is also turned ON at t_2 . The inductor current in winding N_1 starts increasing again. At time t_3 , the sawtooth signal and V_{ctrl2} crossover, which terminates the ON period of Q_1 for the second time. The inductor current in winding N_1 commutes to winding N_2 and starts decreasing and drops to zero at time t_4 . Before the start of the next switching cycle, there is a small time interval $[t_4-t_5]$ to maintain the DCM operation.

 I_{O1} I_{D1} I_{D2} $G_{Q2} \\$ t_1 t₂ t₃ t₄ t₅ t_0

Fig. 8. Gate driving generating scheme for Q_1 and Q_2

TABLE III SIMULATED POWER FACTOR PERFORMANCE OF THE PROPOSED LED DRIVER UNDER 110 VRMS INPUT

Vol_rip / VLED	5%	10%	20%	30%	40%
Power factor $(V_{aux} = 20 V)$	0.99	0.98	0.93	0.85	0.7
Power factor $(V_{aux} = 30 V)$	0.99	0.99	0.96	0.90	0.78
Power factor $(V_{aux} = 40 V)$	0.99	0.99	0.97	0.92	0.84
Power factor $(V_{aux} = 50 V)$	0.99	0.99	0.97	0.94	0.88

V. DESIGN CONSIDERATIONS AND EXAMPLE DESIGN PROCEDURES

In this section, the design considerations for the MRC LED driver will be discussed and an example design procedure will also be presented.

A. V₀₁ Ripple Versus Input Current Distortion

EnergyStar requires power factor implementation for LED drivers with greater than 5 W output. In the proposed design, the interval II input current introduces distortion, which inevitably affects the power factor performance. A model to simulate the average input current of the proposed LED driver has been built. The power factor performance simulation is based on 110 Vrms input, and the results are shown in Table III. To normalize the result, the voltage ripple of V_{o1} is presented as the ratio of $V_{o1_rip}/V_{\text{LED}}$, where V_{o1_rip} is the ripple voltage amplitude of V_{o1} . Note that the dc amplitude of V_{o2} V_{o2} dc is designed based on the minimum requirement to be just enough to maintain V_{o2} above zero. Therefore, in the proposed design, there is $V_{o2_dc} =$ $V_{o1_rip} = V_{o2_rip}$. In this way, the average power delivered to V_{o2} is minimized and so is the input current distortion. In a real design, V_{o2_dc} can be designed slightly higher than V_{o1_rip} to provide a reasonable margin.

As shown in Table III, the power factor of the proposed LED driver is reduced when the ripple ratio V_{rip_vo1}/V_{LED} is increased. Under the same ripple ratio, the power factor is improved when V_{aux} is increased from 20 to 50 V. The improvement is not obvious when the ripple ratio is low, for example, when the ripple ratio V_{o1_rip}/V_{LED} is 5% or 10%. The improvement becomes obvious when the ripple ratio is high. For example, when $V_{o1_rip}/V_{\rm LED} = 40\%$, the power factor is improved from 0.7 when $V_{aux} = 20$ V to 0.88 when $V_{aux} = 50$ V.

In addition to the power factor requirement, IEC61000-3-2 class C sets limit on the input harmonic currents for lighting devices with greater than 75 W power. Two sources contribute to input current distortion, the ac input current during the interval II operation and the ac input current zero-crossing distortion caused by the addition of V_{aux} . The input harmonic currents are simulated based on 110 Vrms input, 50 V, 1.5 A, 75 W output, and the results are presented in Figs. 9-11.

Fig. 9(a) shows the input harmonic currents with $V_{o1_rip}/V_{\text{LED}} = 5\%$ and $V_{\text{aux}} = 20$ V. Each order of input harmonic current is well below the limit set by IEC-61000-3-2 class C. Fig. 9(b) shows the input harmonic currents when $V_{o1_rip}/V_{\rm LED} = 10\%$. Each order of input harmonic current is still below the limit. However, the 21st- and 23rd-order input harmonic currents are already very close to the 3% limit. Fig. 9(c) shows the input harmonic currents when $V_{o1,rip}/V_{\text{LED}} = 20\%$. The input harmonic currents from the second interval input current contribute significantly to the overall harmonic current. As a result, multiple harmonic currents exceed the limit. Fig. 10(a) shows the input harmonic currents when V_{aux} is designed to be 30 V and $V_{o1_rip}/V_{\text{LED}} = 5\%$. Each order of input harmonic current is also very well below the limit. When $V_{\rm aux}$ is increased to 40 V and $V_{o1_rip}/V_{\text{LED}} = 5\%$, the 11th-order input harmonic current exceeds the 3% limit, as shown in Fig. 11(a). In this case, because of a higher V_{aux} , the zero-crossing distortion is more severe and contributes significantly to the overall harmonic currents.

Input harmonic currents in Figs. 9(a) and 10(a) meet the requirement of IEC-61000-3-2 class C, while the results from other design parameters having harmonic currents exceeding the limit or too close to the limit without enough margin. In general, to reduce the input current harmonic currents, it is preferred to have a small $V_{o1_rip}/V_{\text{LED}}$. The presence of voltage V_{aux} also introduces the zero-crossing distortion. When $V_{o1_rip}/V_{\text{LED}}$ is selected, V_{aux} should also carefully selected so that the harmonic currents from zero-crossing distortion do not contribute significantly to the input harmonic currents.

B. V_{o1} Ripple Versus Output Capacitor C_{o1}

The capacitor C_{o1} serves as the storage capacitor to buffer the imbalanced energy between the ac input and the LED output in a half line cycle. The relationship between C_{o1} and the ripple voltage of V_{o1} can be expressed as

$$C_{o1} = \frac{P_{\text{LED}} \times T_{\text{line}}}{2\pi \times V_{o1_avg} \times V_{o1_rip_pp}}.$$
(37)

Equation (37) reveals that the capacitance of C_{o1} is inversely proportioned to the peak-to-peak ripple voltage of V_{o1} . In other words, if a larger ripple voltage is allowed on V_{o1} , the storage





Fig. 9. Input harmonic currents when $V_{in} = 110$ Vrms, $V_{LED} = 50$ V, $I_{LED} = 1.5$ A, $V_{aux} = 20$ V. (a) $V_{aux} = 20$, $V_{o1_rip}/V_{LED} = 5\%$. (b) $V_{aux} = 20$, $V_{o1_rip}/V_{LED} = 10\%$. (c) $V_{aux} = 20$, $V_{o1_rip}/V_{LED} = 20\%$.



Fig. 10. Input harmonic currents when $V_{in} = 110$ Vrms, $V_{\text{LED}} = 50$ V, $I_{\text{LED}} = 1.5$ V, $V_{aux} = 30$ V. (a) $V_{aux} = 30, V_{o1_rip}/V_{\text{LED}} = 5\%$. (b) $V_{aux} = 30, V_{o1_rip}/V_{\text{LED}} = 10\%$. (c) $V_{aux} = 30, V_{o1_rip}/V_{\text{LED}} = 20\%$.



Fig. 11. Input harmonic currents when $V_{in} = 110$ Vrms, $V_{\text{LED}} = 50$ V, $I_{\text{LED}} = 1.5$ V, $V_{\text{aux}} = 40$ V. (a) $V_{\text{aux}} = 40$, $V_{o1_rip}/V_{\text{LED}} = 5\%$. (b) $V_{\text{aux}} = 40$, $V_{o1_rip}/V_{\text{LED}} = 10\%$. (c) $V_{\text{aux}} = 40$, $V_{o1_rip}/V_{\text{LED}} = 20\%$.

capacitor C_{o1} can be smaller. A smaller storage capacitor is preferred in the LED driver design to reduce overall size and even achieve electrolytic capacitor-free design to extend system life. Because of ripple cancellation, flicker-free LED driving can always be achieved, even with a significant ripple voltage present on V_{o1} . Therefore, one of the objectives in the proposed LED driver design is to reduce the capacitor C_{o1} , which also means a large ripple voltage on V_{o1} . One should note that $V_{o1,rip}$ is also linked to the input current distortion discussed earlier. For example, the power factor will be reduced when a larger ripple voltage is presented on V_{o1} . In addition, it will be discussed that the power conversion loss is also related to the ripple voltage, as will be discussed later. Design trade-offs on $V_{o1,rip}$ should be made in order to achieve an overall optimized design.

C. Output Capacitor C_{o2}

The capacitor C_{o2} for the output V_{o2} is used for filtering the switching frequency ripple. It is not required to store energy in a half line cycle. Therefore, a ceramic capacitor can be used in a design. A 22- μ F ceramic capacitor is used in the experimental prototype.

TABLE IV Amount of Power That Goes Through Two Times Power Conversion (Percentage of the Total Output Power)

Vaux	V_{o1_rip} / V_{LED}					
	5%	10%	20%	30%	40%	
20 V	0.03 W	0.06 W	0.14 W	0.25 W	0.46 W	
	(0.4%)	(0.8%)	(1.8%)	(3.3%)	(6.1%)	
30 V	0.04 W	0.12 W	0.21 W	0.37 W	0.66 W	
	(0.5%)	(1.6%)	(2.8%)	(4.9%)	(8.8%)	
40 V	0.06 W	0.15 W	0.27 W	0.49 W	0.85 W	
	(0.8%)	(2%)	(3.6%)	(6.5%)	(11.3%)	
50 V	0.08 W	0.17 W	0.36 W	0.68 W	1.04 W	
	(1%)	(2.2%)	(4.8%)	(9%)	(13.8%)	

D. Vo1 Ripple Versus Conversion Loss

As discussed earlier, it is preferred to have a large ripple voltage $V_{o1,rip}$ to minimize the output capacitor C_{o1} . However, a large ripple voltage $V_{o1,rip}$ will also reduce the power factor performance. To maintain a reasonably good power factor, V_{aux} should be increased along with $V_{o1,rip}$. For example, as shown in Table III, the power factor is increased from 0.7, when $V_{aux} = 20$, to 0.88, when $V_{aux} = 50$ V. Therefore, it can be understood that to maintain a high power factor, V_{aux} should be increased when a higher ripple voltage $V_{o1,rip}$ is to be allowed in the proposed design.

When V_{aux} is not active, the energy is delivered from the ac input directly to output V_{o1} and V_{o2} , respectively. Therefore, this part of energy only goes through one-time power conversion. On the other side, when V_{aux} is active, the energy provided to V_{o2} is processed twice, from the ac input to V_{aux} first and then from V_{aux} to V_{o2} .

The amount of energy provided by V_{aux} to V_{o2} is related to both the ripple voltages V_{o1} and V_{aux} , as indicated by (7). A larger V_{aux} will lead to a longer timespan that V_{aux} is active. At the same time, a larger ripple V_{o1} means a larger V_{o2_avg} . Therefore, more energy will be transferred from V_{aux} to V_{o2} and more energy goes through two power conversion steps. The amount of power being processed twice is calculated, and the result is shown in Table IV, under 110 Vrms input, 7.5 W output with different V_{o1_rip}/V_{LED} and V_{aux} .

As shown in Table IV, to reduce the amount of energy being processed twice to maintain high efficiency, the ripple voltage of V_{o1} should be reduced. Therefore, multiple design considerations are related to $V_{o1,rip}$ and design trade-offs are necessary.

On the other side, the amount of power going through two times power conversion is much higher in the previous ripple cancellation LED drivers, in which the percentage of power that must be processed twice is directly proportional to the ripple ratio $V_{o1_rip}/V_{\text{LED}}$. For example, a 30% $V_{o1_rip}/V_{\text{LED}}$ in the previous ripple cancellation LED driver means 30% output power goes through two times power conversion. The amount of energy going through two times power conversion is much less in this new proposed LED driver when $V_{o1_rip}/V_{\text{LED}}$ is 30%. For example, as shown in Table IV, when $V_{\text{aux}} = 30\%$, the amount of power being processed twice is 4.6% of the total output power while 0.9 power factor can still be achieved under this arrangement, as shown in Table III.

E. Selection of C_{aux}

As discussed in Section II, (5) can be used to calculate the energy supplied by V_{aux} . C_{aux} can be selected based on the voltage change on V_{aux} when it supplies energy to the LED load. The relationship between C_{aux} , E_{aux} , V_{aux} , and the voltage change on $V_{\text{aux}} \Delta V_{\text{aux}}$ can be expressed as

$$E_{\rm aux} = \frac{1}{2} C_{\rm aux} V_{\rm aux}^2 - \frac{1}{2} C_{\rm aux} (V_{\rm aux} - \Delta V_{\rm aux})^2 \qquad (38)$$

where $\triangle V_{aux}$ represents the voltage drop on V_{aux} when it supplied energy to the output. Rearranging (38) yields

$$C_{\rm aux} = \frac{2E_{\rm aux}}{V_{\rm aux}^2 - (V_{\rm aux} - \Delta V_{\rm aux})^2}.$$
 (39)

Under the condition $V_{\text{aux}} = 30 \text{ V}$, $V_{in} = 110 \text{ Vrms}$, $V_{o2_avg} = 2.5 \text{ V}$, and $I_{\text{LED}} = 0.15 \text{ A}$, E_{aux} is calculated to be 0.3 mJ by (5). Using (39) and assuming $\Delta V_{\text{aux}} = 2 \text{ V}$, the capacitor C_{aux} is calculated to be 5.2 μ F.

F. Maintain DCM Operation

DCM operation is needed to ensure interval I input current follows the input voltage. In other words, $[t_0-t_4]$ should be smaller than the predefined switching period T_s . Since the expressions of (t_1-t_0) , (t_2-t_1) , (t_3-t_2) , and (t_4-t_3) have been derived, the total time (t_4-t_0) can be expressed as

$$(t_{4} - t_{0}) = (t_{1} - t_{0}) + (t_{2} - t_{1}) + (t_{3} - t_{2}) + (t_{4} - t_{3})$$

$$= \frac{1}{V_{in.rms}} \sqrt{2 \times P_{in.avg} \times T_{s} \times L_{N1}} + \frac{V_{in.rec}}{V_{o1}}$$

$$\times \frac{1}{V_{in.rms}} \sqrt{2 \times P_{in.avg} \times T_{s} \times L_{N1}}$$

$$+ \frac{1}{V_{in.rec}} \times \sqrt{2 \times I_{\text{LED}} \times V_{o2} \times T_{s} \times L_{N1}}$$

$$+ \sqrt{\frac{2 \times I_{\text{LED}} \times T_{s} \times L_{N1}}{V_{o2}}} \times \frac{N_{2}}{N_{1}}.$$
(40)

Equation (40) is only valid when $T_s > (t_4-t_0)$, and this should be verified for a proposed design. With known P_{in_avg} , T_s , L_{N1} , V_{in_rms} , I_{LED} , V_{o1} , V_{o2} , and $N_2:N_1$, the time (t_4-t_0) can be calculated and plotted in a half line cycle. An ideal $(t_4-t_0)_{\text{max}}$ should be just slightly smaller than T_s . For example, $(t_4-t_0)_{\text{max}} = 48 \,\mu\text{s}$ and $T_s = 50 \,\mu\text{s}$. In this way, DCM operation can be maintained all the time and the component current stresses are minimized. Further adjusting $(t_4-t_0)_{\text{max}}$ can be achieved by changing L_{N1} as (t_4-t_0) is proportional to the square root of L_{N1} .

G. Example Design Procedure

An example design procedure is presented as follows:

- Step 1: Select the switching frequency. To reduce switching loss, it is preferred to reduce the switching frequency for low-power designs. Twenty kilohertz switching frequency can be selected to minimize switching loss while avoiding audible switching noise.
- Step 2: Select the output capacitor C_{o1} . On one side, it is desirable to reduce the storage capacitor to minimize the

size of LED drivers and even achieving electrolytic capacitor-less designs. On the other side, a smaller C_{o1} will lead to a higher voltage ripple $V_{o1,rip}$, which further leads to a higher input current distortion and more conversion loss. Therefore, design trade-offs on selecting C_{o1} should be made to achieve an overall optimized design. In particular, for higher than 75 W output power design, IEC 61000-3-2 class C sets the limit for input harmonic currents. It is more critical to select C_{o1} to meet the input harmonic current requirement than to reduce capacitor size.

- Step 3: Select the voltage V_{aux} . For less than 75 W output power designs, the power factor performance is one of the major concerns. A higher V_{aux} can be used to improve the power factor correction performance. For higher than 75 W output power designs, the presence of V_{aux} also contributes to the input harmonic currents. A higher V_{aux} does not necessarily reduce the input harmonics current and can even lead to increased input current harmonics. $V_{\rm aux}$ should be selected to achieve an overall minimal harmonic current. Fig. 12 shows an example of input harmonic currents under different V_{aux} . In Fig. 12(a), because V_{aux} is small, the interval II input current dominates the harmonic contents. In Fig. 12(c), with a high V_{aux} , the zero-crossing distortion harmonics dominant. Comparing the results in Fig. 12(a), (b), and (c), Fig. 12(b) presents the best result, with each order of harmonic current far below the limit. If no $V_{\rm aux}$ can be found to meet the IEC-61000-3-2 class C requirement, it is an indication that V_{o1_rip} is too large in the design. In this way, one needs to go back to step 2 to select a larger C_{o1} to reduce V_{o1_rip} .
- Step 4: Select the turns ratio $N_1:N_2$. As shown in Tables I and II, the voltage and current stresses of Q_2 and D_2 are closely related to the turns ratio $N_1:N_2$. In addition, (14) places one more restriction on the turns ratio, which is $N_1:N_2 < V_{o1}:V_{o2}$. In the experimental prototype, $N_1:N_2 = 8:1$ is selected to keep the voltage stresses of Q_2 and D_2 being around 20 V. In this way, low-voltage-rating components can be selected for D_2 and Q_2 .
- Step 5: Select the inductance L_{N1} . To maintain DCM operation, L_{N1} should be selected to make $(t_4-t_0)_{\text{max}}$ smaller than T_s . At the same time, it is desirable to have a larger L_{N1} . As indicated in (28) and (32), a larger L_{N1} reduces the current stresses of Q_1 , D_1 , Q_2 , and D_2 . In the experimental prototype, L_{N1} is designed to be 1.25 mH.
- *Step 6:* Final parameter adjustment. Steps 4 and 5 can be repeated for a few iterations until a satisfying set of parameters is obtained.

VI. COMPARISON BETWEEN DIFFERENT LED DRIVING TECHNOLOGIES

In this section, a comparison between different LED driving technologies will be made and the result is summarized in Table V. A conventional single-stage LED driver can achieve high efficiency since only one power conversion step is required. The other advantages of conventional single-stage LED drivers include low cost, low-input harmonic currents, and high power factor. However, it is very difficult, almost impossible, to achieve flicker-free LED driving performance. The output ripple voltage of a single-stage LED driver, which is caused by the imbalanced energy between input and output, is applied to the LED load directly and produces significant ripple LED current, which causes lighting flicker. Large storage capacitors are also required by a single-stage LED driver to buffer the imbalanced energy between the ac input and the dc LED output.

A conventional two-stage LED driver can achieve flickerfree LED driving, high power factor, and low-input harmonic currents. The first stage performs power factor correction while the second-stage regulates the LED current. However, due to two stages of power conversion, the component cost is high and the efficiency is relatively low.

The previous ripple cancellation LED driver can achieve flicker-free LED driving, high power factor, and low-input harmonic currents. The amount of power that goes through two times power conversion is related to the voltage amplitude of the ripple cancellation voltage. The efficiency of a ripple cancellation LED driver is between the efficiency of a single-stage LED driver and a two-stage LED drive. There is a small extra cost to build the ripple cancellation converter. The required storage capacitor for a previous ripple cancellation LED driver is much lower than a single-stage LED driver.

The proposed multiplexing ripple cancellation LED driver can achieve high efficiency and flicker-free LED driving. The unique operation distorts the input current from its ideal form. However, an optimized design can be achieved with significantly reduced storage capacitor, reasonably good power factor performance, and high efficiency.

VII. EXPERIMENTAL VERIFICATIONS

To verify the proposed MRC LED driver, a 7.5-W experimental prototype was designed based on the procedure presented in previous section, built, and tested. Table VI gives the design specification and the circuit parameter of the experimental prototype.

Fig. 13 shows the ripple cancellation waveforms of the proposed MRC LED driver. The double-line-frequency ripple voltage on the output V_{o1} is 2 V peak to peak. Due to grounding requirement, $-V_{o2}$ is measured in Fig. 13 instead of V_{o2} . The output $-V_{o2}$ has an in phase ripple voltage to cancel the ripple voltage from V_{o1} . In this way, the double-line-frequency ripple voltage on the LED is greatly reduced. The double-linefrequency ripple LED current is measured to be 16 mA peak to peak, which means 8 mA peak and the ripple current is 5.3% of the average LED current. Note that the occasional spikes on the LED current are excluded in the measurement. There are also noticeable voltage spikes on V_{o2} caused by noise. The noisy natural of buck-boost operation introduced significant noise, which disturbs the voltage regulation loop of V_{o2} . The voltage spikes can be reduced or eliminated when a better layout is designed.



Fig. 12. Simulated harmonic input current of the proposed MRC LED driver under different V_{aux} ($V_{in} = 110$ Vrms, $V_{o2_min} = 0.5$ V, $V_{o2_max} = 2.5$ V, $V_{LED} = 50$ V, $I_{LED} = 0.15$ A, $P_{out} = 7.5$ W). (1a) $V_{aux} = 10$ V. (2a) $V_{aux} = 20$ V. (3a) $V_{aux} = 30$ V. (1b) $V_{aux} = 10$ V. (1b) $V_{aux} = 20$ V. (1c) $V_{aux} = 30$ V.

 TABLE V

 Comparison Between Different LED Driving Technologies

Topology	Power processed	Efficiency	Required storage capacitor	Flicker-free LED driving	Power factor performance	Input harmonic currents	Cost
Single-stage LED driver	100% output power is processed one time	High	High.	No	High	Low	Low
Two-stage LED driver	100% output power is processed two times	Low	High	Yes	High	Low	High
Previous ripple cancellation LED driver	90% output power is processed one time and 10% output power is processed two times (when $V_{o1_{rip}} / V_{LED} = 10\%$)	Intermedia te to high	Low	Yes	High	Low	Intermediate
Proposed multiplexing ripple cancellation LED driver	99.2% output power is processed one time and 0.8% output power is processed twice ($V_{ol_rip} / V_{LED} = 10\%$ and $V_{aux} = 20$ V)	High	Low	Yes	Intermediate to high	Intermediate	Intermediate

Fig. 14 shows the gate driving and the switching current waveforms of the MRC LED driver. A switching cycle starts at time t_0 when MOSFET Q_1 is turned ON. The magnetic current in winding N_1 (and Q_1) starts rising from zero. The magnetic current peaks at t_1 when Q_1 is turned OFF, and it continues flowing in D_1 . The magnetic current drops to zero before the time t_2 , which ends the interval I operation. MOSFET Q_1 is turned ON at t_2 again and the magnetic current in winding N_1 starts increasing from zero again. The current peaks at t_3 when Q_1 is turned OFF. The magnetic current then commutes from winding N_1 to winding N_2 and continues its flow in diode D_2 and MOSFET Q_2 . The current in winding N_2 drops to zero at time t_4 , which ends the interval II operation.

Fig. 15 shows the voltage stresses of Q_1 , Q_2 , and D_2 in the experimental prototype. The input current waveform and the output voltage waveforms are also included to reflect the full-load operating condition. The maximum voltage of Q_1 is around 190 V. The voltage stresses of Q_1 in the LED driver is the same as it is in a conventional buck–boost LED driver. The voltage across the anode of diode D_2 and the source of Q_2 is measured. When the voltage is positive, it indicates D_2 is forward biased while the body diode of Q_2 is reversely biased. Vice versa, it

TABLE VI DESIGN SPECIFICATION AND CIRCUIT PARAMETER

Design specification					
Input voltage	89 Vrms – 132 Vrms				
V _{LED}	$\sim 50 \text{ V}$				
I _{LED}	0.15 A				
Circuit parameter					
Coupled inductor	$N_1: N_2 = 8:1, L_{N1}=1.25 \text{ mH}$ EE16 core				
Main MOSFET Q1	2SK2803 (450 V 3 A)				
Main output diode D ₁	LQA06T300 (300 V 6 A)				
MOSFET Q ₂	ZXMN4A06GTA (40 V 5 A)				
Output diode D ₂	MBRS340T3G (40 V 4 A)				
Capacitor Caux	ECA-1HM470B (47 μF, 50 V)				
Output capacitor	EKZE101ELL271MK30S				
Col	(270 µF, 100 V)				
Output capacitor C ₀₂	CL21A226KOQNNNE (22 μF, 16 V)				
LED current sensing resistor	KNP100JR-73-0R5 (0.5 ohm)				
Controller	PIC16F1578-I/SS				
Switching frequency fs	20 kHz				



Fig. 13. Ripple cancellation waveforms of the proposed MRC LED driver: (a) experimental result and (b) simulated result with the PSIM 11.0 version.



Fig. 14. Key switching waveform of the MRC LED driver.



Fig. 15. Power components voltage stresses of the MRC LED driver: (a) measured result and (b) simulated result with PSIM 11.0 version.

indicates D_2 is reversely biased while the body diode of Q_2 is forward biased. Therefore, as shown in Fig. 15, the maximum voltage on D_2 is around 6 V while the maximum voltage on Q_2 is around 20 V.

Fig. 16 shows the efficiency of the proposed MRC LED driver with and the efficiency of a conventional single-stage buckboost LED driver. The efficiency of MRC prototype is 1% lower than the efficiency of a conventional LED driver. This is due to extra switching loss with the second interval operation. Overall, this is a very small price to pay when flicker-free LED driving



Fig. 16. Efficiency of the experimental prototype LED driver with/without RCU under full-load condition (red line: without RCU; blue line: with RCU).



Fig. 17. Power factor correction performance of the MRC LED driver.



Fig. 18. Input current harmonics of the proposed MRC LED driver under 110 Vrms input.

performance is achieved. On the other hand, to achieve flickerfree LED driving performance and the same efficiency with a two-stage LED driver, the second-stage dc–dc converter needs to achieve 99% efficiency, which is not realistic to achieve with a conventional design. Assuming the second-stage buck converter achieves 95% efficiency, the final efficiency of the two-stage LED driver will be $85\% \times 0.95 = 80.7\%$, which is significantly lower than the proposed LED driver.

Fig. 17 shows the power factor correction performance of the proposed MRC LED driver. Around 0.98 PF has been achieved



Fig. 19. 7.5-W MRC LED driver experimental prototype.

under full load condition. Fig. 18 shows the input current harmonics of the proposed LED driver. The experimental results show that the converter is able to meet the requirements outlined by IEC 61000 3 2 class C, however, the 9th- and 11th-order harmonic currents are very close to the limit. It is expected that the input current harmonics can be further reduced with an optimized input filter design.

Fig. 19 shows the photo of the experimental prototype.

VIII. CONCLUSION

In this paper, an MRC LED driver is proposed to achieve flicker-free LED driving, high efficiency, and a high power factor correction. The power circuit is operated in time multiplexing manner with two intervals in one switching cycle. The operation in interval I performs power factor correction and transfers energy from the ac input to the LED load. The operation in interval II produced the opposite ripple voltage to achieve ripple cancellation. The proposed MRC LED driver also achieves true single-stage power conversion, improving efficiency over previous ripple cancellation LED driver. One sacrifice of achieving single-stage power conversion is an increased input harmonic current. With a proper design parameter, the input current harmonics can be limited to meet the requirement of IEC-61000-3-2 class C. The LED driver can maintain a low cost by minimizing additional components, making it a very competitive solution for cost-sensitive low-power designs. A 7.5 W experimental prototype had been built and tested to verify the operation of the LED driver. The experimental prototype achieves 0.98 PF, 5.3% of double-line-frequency ripple LED current performance while the efficiency is only 1% efficiency lower than a conventional buck-boost LED driver.

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Peng Fang (S'11–M'16) received the M.Sc. degree from the Hong Kong University of Science and Technology, Hong Kong, in 2007, and the Ph.D. degree from Queen's University, Kingston, ON, Canada, in 2016.

From 2007 to 2011, he was a Power Electronics Engineer with ASM Pacific Technology, Hong Kong, where he led the designs of power converters and power amplifiers. After he graduated from Queen's University, he continued his research in the same research lab as a Postdoctoral Research Fellow

from 2016 to 2018. Since 2018, he has been an Assistant Professor with the Department of Electrical Engineering, University of Minnesota, Duluth, MN, USA. He has two granted U.S. patents and another four U.S. patents in pending. His current research interests include LED driver, EV charger, wireless power transfer, smart grid, and ultra-high-frequency power converter design.



Samuel Webb (S'17) received the B.S. degree in 2016 from Queen's University, Kingston, ON, Canada, where he is currently working toward the Ph.D. degree.

His current research interests include extremely high-efficiency dc/dc converters for point-of-load applications.



Yang Chen (S'14–M'17) received the B.Sc. and M.Sc. degrees in electrical engineering from the Beijing Institute of Technology, Beijing, China, in 2011 and 2013, respectively, and the Ph.D. degree in electrical and computer engineering from Queen's University, Kingston, ON, Canada, in 2017.

He is currently with Queen's University. His current research interests include topology and control of power converters for datacenter and server power supplies, miniaturized resonant converters for notebook and cellphone fast chargers, and high-performance

dc-dc converters with wide voltage range and ac-dc chargers for EVs. He is the author of 20 technical papers published in the IEEE Transactions and conferences and has six U.S./PCT patents pending.



Yan-Fei Liu (F'13) received his bachelor's and master's degrees from Zhejiang University, China, in 1984 and 1987 and Ph.D. degree from Queen's University, Kingston, ON, Canada, in 1994.

He was a Technical Advisor with the Advanced Power System Division, Nortel Networks, in Ottawa, Canada from 1994 to 1999. Since 1999, he has been with Queen's University, where he is currently a Professor with the Department of Electrical and Computer Engineering. His current research interests include optimal application of GaN and SiC devices to

achieve small size and high efficiency power conversion, 99% efficiency power conversion with extremely high power density, digital control technologies for high efficiency, fast dynamic response dc–dc switching converter and ac–dc converter with power factor correction, resonant converters and server power supplies, and LED drivers. He has authored around 250 technical papers in the IEEE Transactions and conferences, and holds 35 U.S. patents. He has written a book on "High Frequency MOSFET Gate Drivers: Technologies and Applications," published by IET. He is also a Principal Contributor for two IEEE standards. He received "Modeling and Control Achievement Award" from IEEE Power Electronics Society in 2017. He received Premier's Research Excellence Award in 2000 in Ontario, Canada. He also received the Award of Excellence in Technology in Nortel in 1997.

Dr. Liu is the Vice President of Technical Operations of IEEE Power Electronics Society (PELS, from 2017 to 2020). Dr. Liu serves as an Editor of IEEE JOURNAL OF EMERGING AND SELECTED TOPICS OF POWER ELECTRONICS (IEEE JESTPE) since 2013. He is the General Chair of ECCE 2019 to be held in Baltimore, USA in 2019. His major service to IEEE is listed below: a Guest Editor-in-Chief for the special issue of Power Supply on Chip of IEEE TRANS-ACTIONS ON POWER ELECTRONICS from 2011 to 2013; a Guest Editor for special issues of JESTPE: Miniaturization of Power Electronics Systems in 2014 and Green Power Supplies in 2016; as Co-General Chair of ECCE 2015 held in Montreal, Canada, in September 2015; the Chair of PELS Technical Committee (TC1) on Control and Modeling Core Technologies from 2013 to 2016; Chair of PELS Technical Committee (TC2) on Power Conversion Systems and Components from 2009 to 2012.



Paresh C. Sen (M'67–SM'74–F'89–LF'04) was born in Chittagong, Bangladesh. He received the B.Sc. (with honors in physics) and the M.Sc. (Tech.) degrees in applied physics from the University of Calcutta, Kolkata, India, in 1958 and 1962, respectively, and the M.A.Sc. and Ph.D. degrees in electrical engineering from the University of Toronto, Toronto, ON, Canada, in 1965 and 1967, respectively.

He is currently an Emeritus Professor of Electrical and Computer Engineering at Queen's University, Kingston, ON, Canada. He has worked for industries

in India and Canada and was a consultant to electrical industries in Canada. He has authored or coauthored over 215 technical papers in the general area of electric motor drives and power electronics. He is the author of two internationally acclaimed textbooks: *Principles of Electric Machines and Power Electronics* (Wiley, 1989, 1997, 2013) and *Thyristor DC Drives* (Wiley, 1981). He was engaged in teaching electric machines, power electronics, and electric drive systems for over 45 years. His current research interests include power electronics, electric drive systems, switching power supplies, wind energy systems, digital control, and modern control techniques for power electronics and motor drive systems.

Dr. Sen has served IEEE in various capacities: as an Associate Editor, Distinguished Lecturer, Chairman of the Technical Committees on power electronics and energy systems, Session Organizer, Session Chairperson, and Paper Reviewer. He served as an NSERC (Natural Science and Engineering Research Council of Canada) Scientific Liaison Officer evaluating university-industry coordinated projects. He is globally recognized as an authority in power electronics and motor drive systems. He received the IEEE-IAS (Industry Application Society) Outstanding Achievement Award in 2008 and the IEEE-Canada Outstanding Engineering Educator Award in 2006 for his outstanding contributions over four decades as a researcher, supervisor, teacher, author, and consultant. He received the IAS-IDC Prize Paper Award in 1986. He is a Fellow of the EIC. As an Emeritus Professor, he continues to be active in research and supervision of graduate students and in several IEEE societies.